1. Given the public key (N, e) = (3127,17)
   1. To find all M such that M = C, we need to find Me such that Me mod N = C and since C = M which implies to us that Me mod N = M. This can be the same thing as Me mod N = M. This means we need to find M such that M17 mod 3127 = M. We also know that M is in the range 2 till 3126 (as we are finding values for M not being 0 and 1).  
      To accomplish this, we perform repeated squaring for all these values to see when M17 mod 3127 = M mod 3127.  
      Running the program, we get the following values  
       [235, 295, 530, 531, 825, 1061, 2066, 2302, 2596, 2597, 2832, 2892, 3126]
   2. Our smallest value is 235 so in this case we aim to find 23517 mod 3127  
      First we convert 17 into binary which is 1001  
      From here we build the following list from (1,10,100,1001) which is the same as (1,2,4,17)  
      235 = 235 (mod 3127)  
      2352 = 2352 = 55225 = 2066 (mod 3127)  
      2354 = (2352)2 = 20662 = 1 (mod 3127)  
      23517 = (2354 \* 4+1)= (2354 )4 \* (235)= 1\*235 = 235 (mod 3127)
   3. In practice, it shouldn’t be a huge security concern as modulus N is much larger than 3127, especially if we use two very large prime numbers for p and q (Recall p \* q =N). This means that as p and q are large, trying to factor N becomes very hard which means that an attacker will struggle to find the private key d.
2. X: Specified Constant which is public, M is a Single Block Message which is the size of key in block cipher. The hash is Y = E(X,M)
   1. One-Way Property:  
      The one way property is that given Y, is it is hard to find X such that Hash(X) = Y. In this case, given Y is hard to find the message M such that Y = E(X,M). Here we assume the block cipher is secure. As we use the message M in place of the key and X in place of the plaintext, the attackers aim is to get M from X and Y alone since they don’t have access to E. Since they don’t have access to the block cipher, it makes it impossible to retrieve M from this, thus satisfying the condition  
        
      Weak Collision Resistance:  
      Weak Collision Resistance is when given a message M and a hash function, it is unfeasible to find another M’ such that M != M’ but Hash(M)=Hash(M’). So in this case we need to find M!=M’ such that E(X,M) = E(X,M’). As we assume the cipher is secure, based off the properties of a secure block cipher (pseudorandom nature) we know that the hash is weak collision resistant.
   2. Since we have two keys K0 and K1 and that E(P,K0 ) = E(P,K1), this leads to a collision in the hash function. Due to the fact that E(P,K0 ) = E(P,K1), and assuming K0 and K1 are not the same, this means the weak collision resistance property no longer holds thus leading to an insecure hashing method.
   3. To extend the definition of the hash to include a second block, we can change the method to make it Y = E( E( X, M1 ⊕ M2), M2)